

Machine learning for Quantum Noise Benchmarking

Stefano MARTINA
stefano.martina@unifi.it



Quantum Driving And
Bio-complexity



UNIVERSITÀ
DEGLI STUDI
FIRENZE

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Overview

- 1 Introduction
- 2 Setting definition
- 3 Machine Learning
- 4 Results

Introduction


- ✓ We consider a **Quantum Random Walker** on a complex graph
 - ▶ perturbed by noise
- ✓ **Discriminate** quantum noise, by measuring only walker **populations**
 - ▶ Support Vector Machines
 - ▶ Recurrent Neural Networks
- ✓ The **dynamic parameters** are crucial to the classification capacity
 - ▶ short evolution time / high frequency → **easy**
 - ▶ long evolution time / low frequency → **hard**
- ✓ Over **90%** accuracy in classification between
 - ▶ two **IID** noises
 - ▶ two **coloured** noises
 - ▶ one **IID** VS one **coloured** noises

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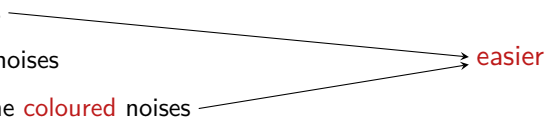
The diagram consists of three lines originating from the right side of the three bullet points in the last list item. These lines converge towards a single arrowhead pointing to the word 'easier' in red text.

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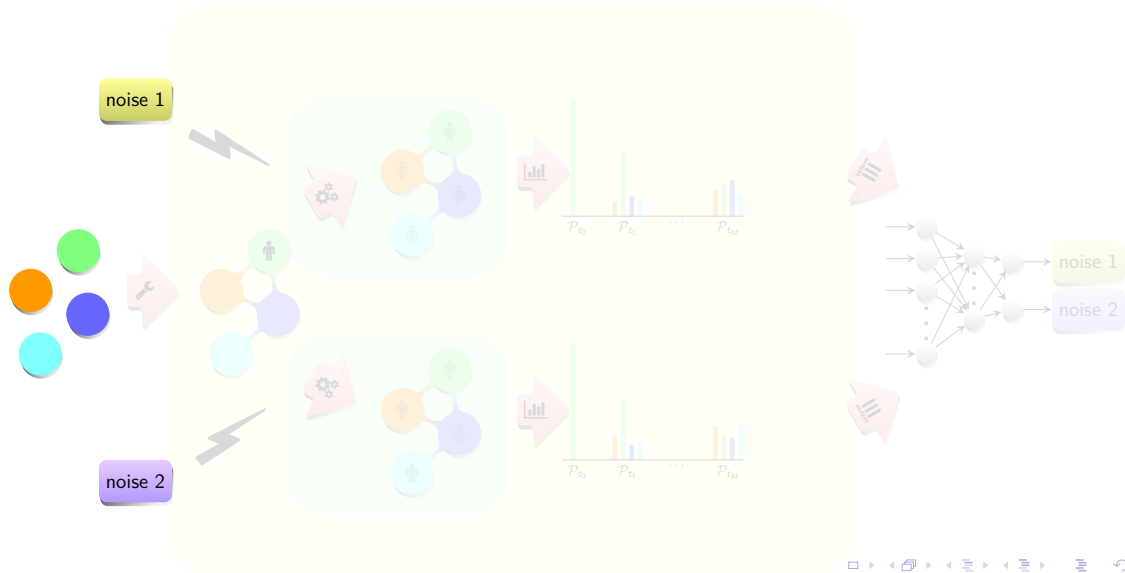
The diagram shows three bullet points from the previous list: 'two IID noises', 'two coloured noises', and 'one IID VS one coloured noises'. Three lines originate from the right side of each bullet point and converge towards the word 'easier' on the right side of the slide.

Introduction

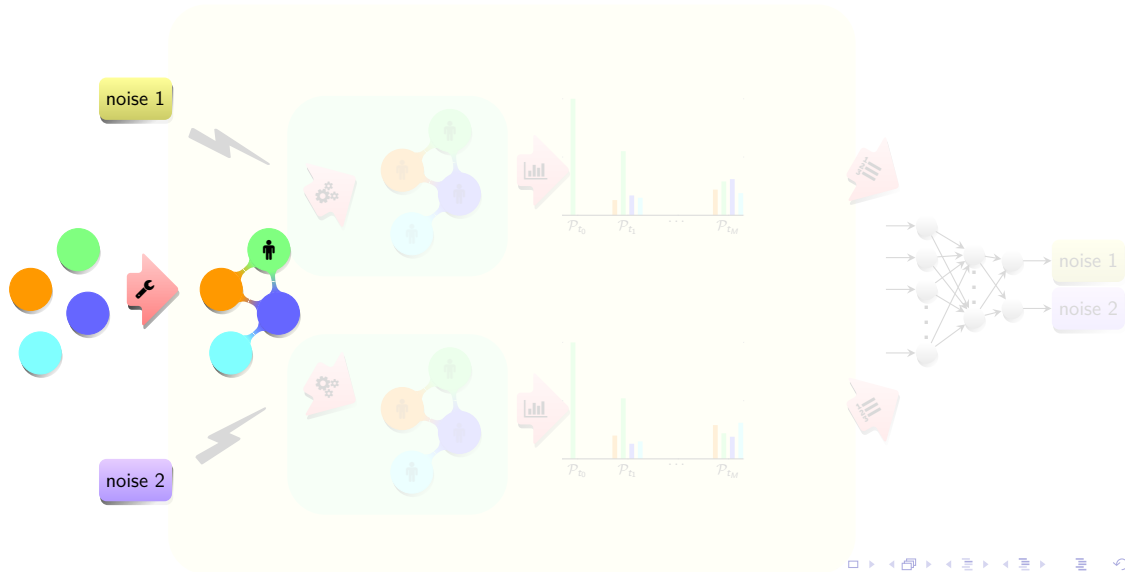
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→ **easier**

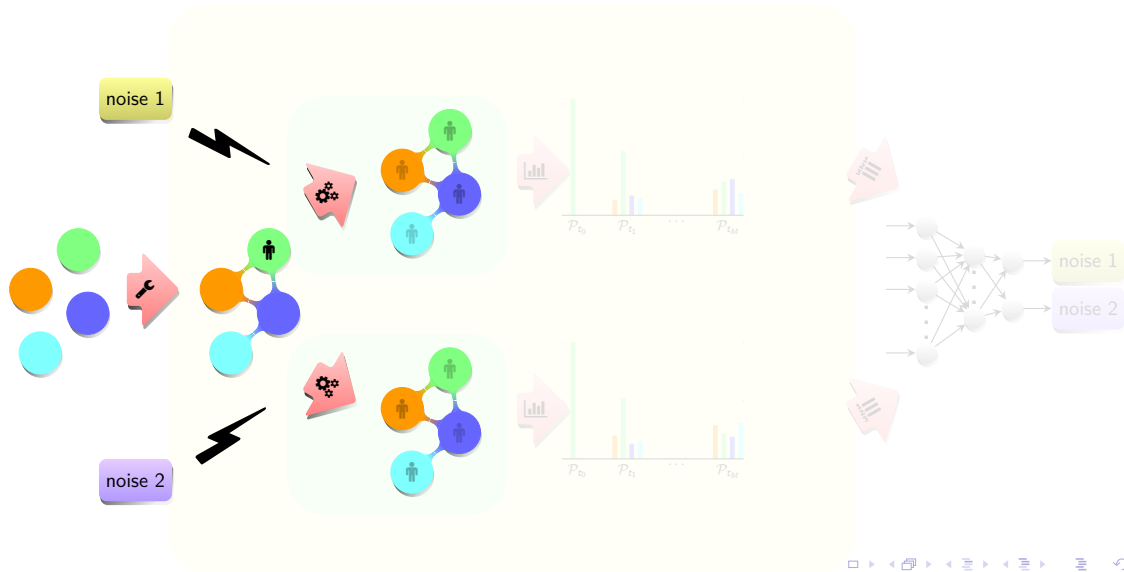
Setting definition



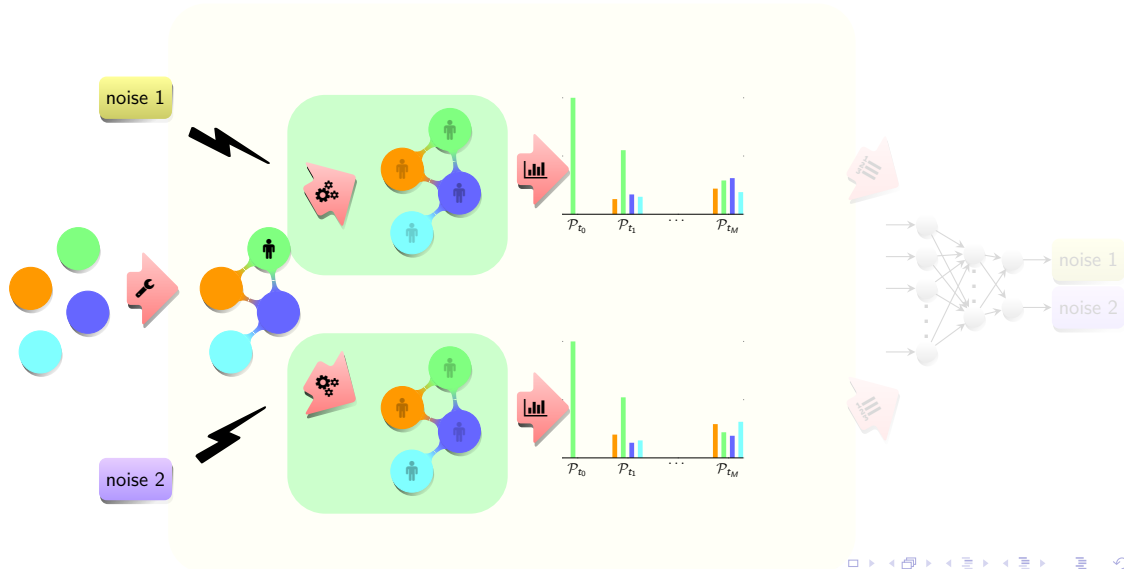
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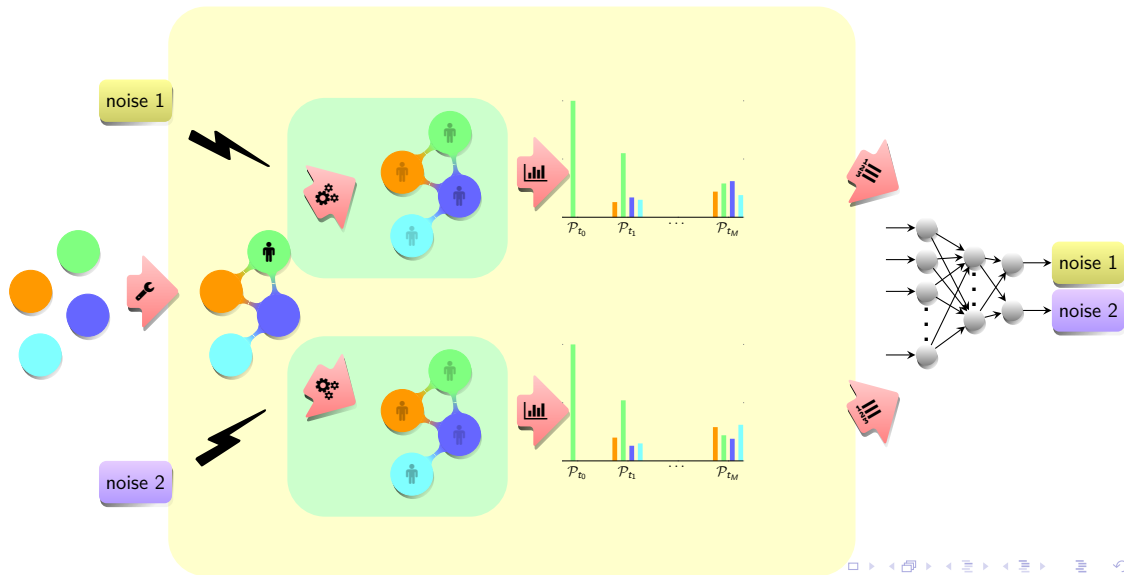
Setting definition



Setting definition



Setting definition



Example

- ✓ Example of populations with $t_{15} = 0.1$

	$\mathcal{P}_{t_k}^{(35)}$	$\mathcal{P}_{t_k}^{(36)}$	$\mathcal{P}_{t_k}^{(37)}$	$\mathcal{P}_{t_k}^{(38)}$	$\mathcal{P}_{t_k}^{(39)}$	$\mathcal{P}_{t_k}^{(40)}$
t_0	0.00	0.00	0.00	0.00	1.00	0.00
t_1	0.00	0.00	0.00	0.00	0.99	0.00
t_2	0.00	0.00	0.00	0.00	0.93	0.00
t_3	0.00	0.00	0.01	0.01	0.85	0.01
t_4	0.00	0.01	0.01	0.01	0.78	0.01
t_5	0.01	0.01	0.01	0.01	0.69	0.01
t_6	0.01	0.02	0.01	0.01	0.63	0.00
t_7	0.01	0.02	0.01	0.01	0.57	0.00
t_8	0.01	0.02	0.01	0.01	0.52	0.00
t_9	0.02	0.02	0.01	0.01	0.45	0.00
t_{10}	0.02	0.02	0.02	0.02	0.37	0.01
t_{11}	0.01	0.02	0.02	0.03	0.29	0.01
t_{12}	0.01	0.01	0.03	0.04	0.20	0.02
t_{13}	0.01	0.01	0.04	0.04	0.14	0.01
t_{14}	0.01	0.02	0.04	0.05	0.08	0.01
t_{15}	0.01	0.02	0.04	0.05	0.06	0.01

- ✓ Example of populations with $t_{15} = 1$

	$\mathcal{P}_{t_k}^{(35)}$	$\mathcal{P}_{t_k}^{(36)}$	$\mathcal{P}_{t_k}^{(37)}$	$\mathcal{P}_{t_k}^{(38)}$	$\mathcal{P}_{t_k}^{(39)}$	$\mathcal{P}_{t_k}^{(40)}$
t_0	0.00	0.00	0.00	0.00	1.00	0.00
t_1	0.02	0.02	0.01	0.01	0.45	0.00
t_2	0.01	0.01	0.02	0.03	0.05	0.02
t_3	0.00	0.00	0.00	0.00	0.13	0.02
t_4	0.02	0.01	0.01	0.01	0.12	0.02
t_5	0.01	0.01	0.03	0.03	0.06	0.01
t_6	0.01	0.01	0.01	0.01	0.01	0.00
t_7	0.04	0.03	0.01	0.06	0.11	0.00
t_8	0.04	0.00	0.03	0.11	0.11	0.03
t_9	0.03	0.00	0.03	0.01	0.01	0.10
t_{10}	0.05	0.01	0.01	0.04	0.08	0.04
t_{11}	0.01	0.03	0.02	0.00	0.08	0.02
t_{12}	0.00	0.05	0.02	0.04	0.00	0.06
t_{13}	0.01	0.03	0.00	0.02	0.05	0.07
t_{14}	0.00	0.00	0.00	0.01	0.12	0.00
t_{15}	0.00	0.00	0.01	0.04	0.10	0.01

Model

$$\hat{\mathbf{y}} = f(\mathbf{x}; \theta, \xi)$$

- ✓ f non-linear function parametrized with
 - ▶ **parameters** θ (modified during training)
 - ▶ **hyperparameters** ξ (define different configurations)

Target

$$\theta^* = \arg \min_{\theta} L_{\mathcal{D}}(\theta, \xi)$$

Theoretical risk function

$$L_{\mathcal{D}}(\theta, \xi) \equiv \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{D}} [\ell(f(\mathbf{x}; \theta, \xi), \mathbf{y})]$$

✓ \mathcal{D} is unknown

Learning II

Target

$$\theta^* = \arg \min_{\theta} L_S(\theta, \xi)$$

Empirical risk function

$$L_S(\theta, \xi) = \frac{1}{|S|} \sum_{(\mathbf{x}, \mathbf{y}) \in S} \ell(f(\mathbf{x}; \theta, \xi), \mathbf{y})$$

- ✓ $S = \{(\mathbf{x}_1, \mathbf{y}_1), \dots, (\mathbf{x}_N, \mathbf{y}_N)\}$ **training** dataset
- ✓ Monitor $L_{S'}(\theta, \xi)$ on **validation** set $S' \neq S$
 - ▶ Detect **overfitting**
 - ▶ Tune hyperparameters ξ
- ✓ Report $L_{S''}(\theta, \xi)$ (and metrics) on **test** set $S'' \neq S' \neq S$

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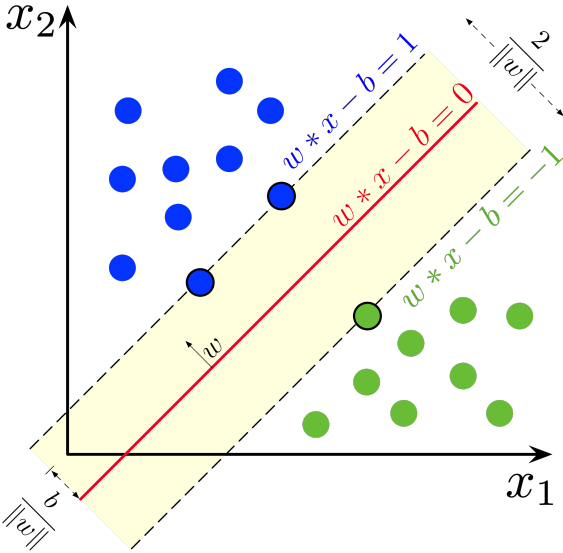
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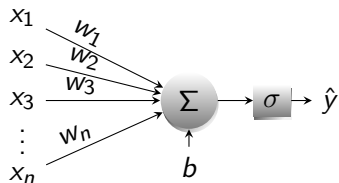
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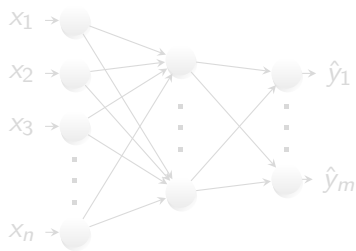
Support Vector Machines



Multi Layer Perceptron



$$\hat{y} \equiv \sigma(\mathbf{w}^T \cdot \mathbf{x} + b)$$

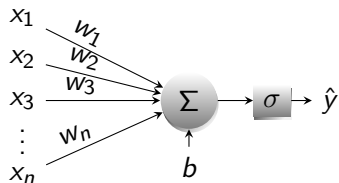


$$\mathbf{h}[0] \equiv \mathbf{x}$$

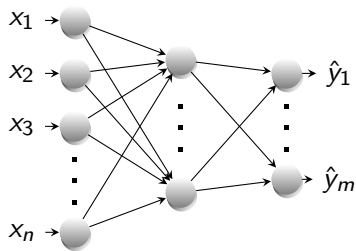
$$\mathbf{h}[l] \equiv \sigma \left(W[l]^T \cdot \mathbf{h}[l-1] + \mathbf{b}[l] \right)$$

$$\hat{\mathbf{y}} \equiv \mathbf{h}[L]$$

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Categorical Cross Entropy

$$\ell(\hat{\mathbf{y}}, \mathbf{y}) = - \sum_{j=1}^O y^{(j)} \log \hat{y}^{(j)}$$

- ✓ Common used in **classification** tasks
- ✓ Measure distance between two probability distributions
 - ▶ $\hat{\mathbf{y}}$ needs to be a probability distributions
 - ▶ obtained with **softmax** function:

$$\sigma^{(i)}(\mathbf{z}) \equiv \frac{e^{z^{(i)}}}{\sum_{j=1}^O e^{z^{(j)}}}$$

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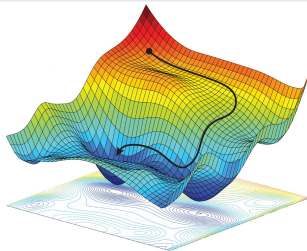
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Stochastic Gradient Descent

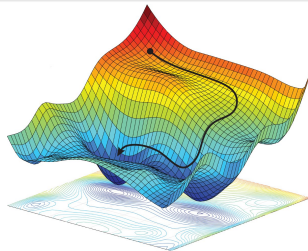
$$\theta_i = \theta_{i-1} - \eta \nabla_{\theta} L_{S_b}(\theta_{i-1}, \xi)$$



- ✓ η is the learning rate
 - ▶ Can also be adaptively updated (e.g. ADAM)
- ✓ S_b is a minibatch

Stochastic Gradient Descent

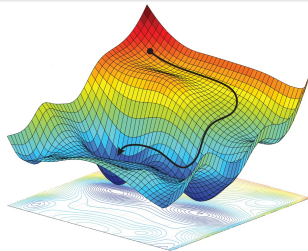
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Unidirectional Recurrent Neural Network (RNN)

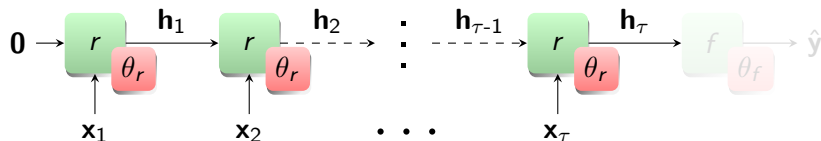


$$\mathbf{h}_t = r(\mathbf{x}_t, \mathbf{h}_{t-1}; \theta_r)$$

$$\hat{\mathbf{y}} = f(\mathbf{h}_{\tau}; \theta_f)$$

- ✓ Used on **sequential** data
- ✓ Processed iteratively by **non-linear** function r
 - ▶ r parametrized with **shared** set of weights θ_r
 - ▶ \mathbf{h}_t sort of **memory**
- ✓ \mathbf{h}_{τ} **representation** of all the sequence
 - ▶ In **classification** \mathbf{h}_{τ} can be processed by MLP f

Unidirectional RNN

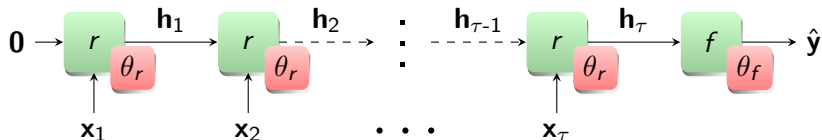


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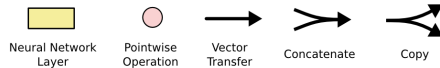
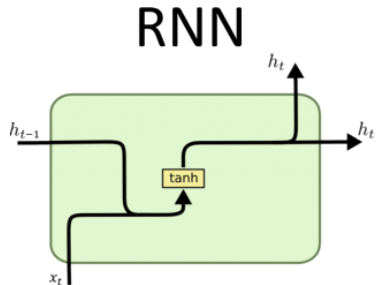


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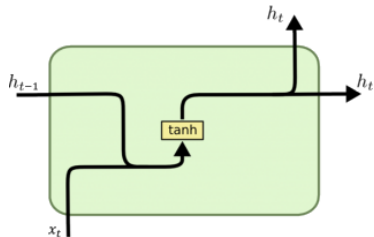
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GRU/LSTM

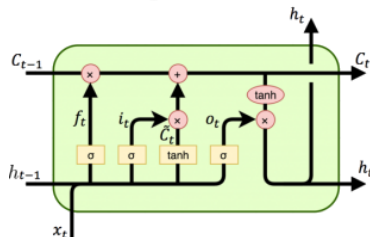


GRU/LSTM

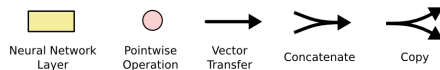
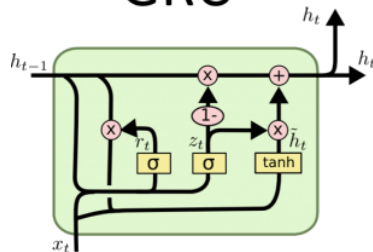
RNN



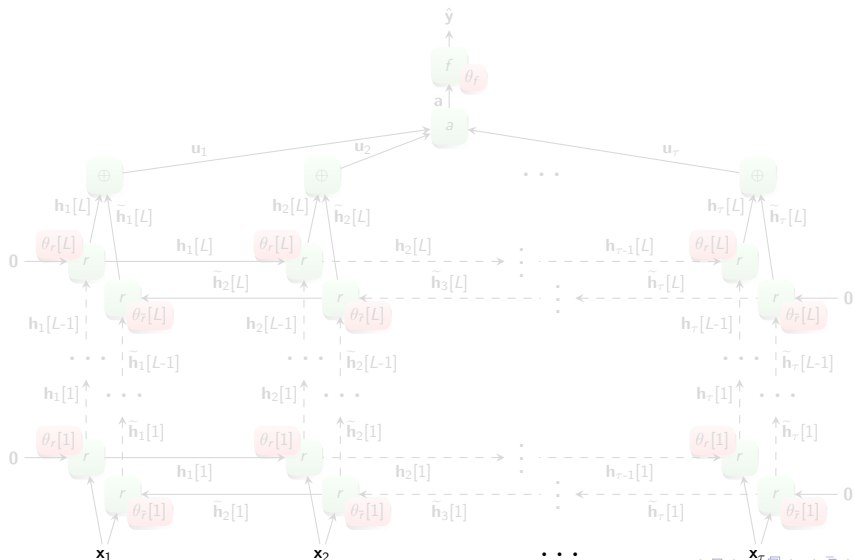
LSTM



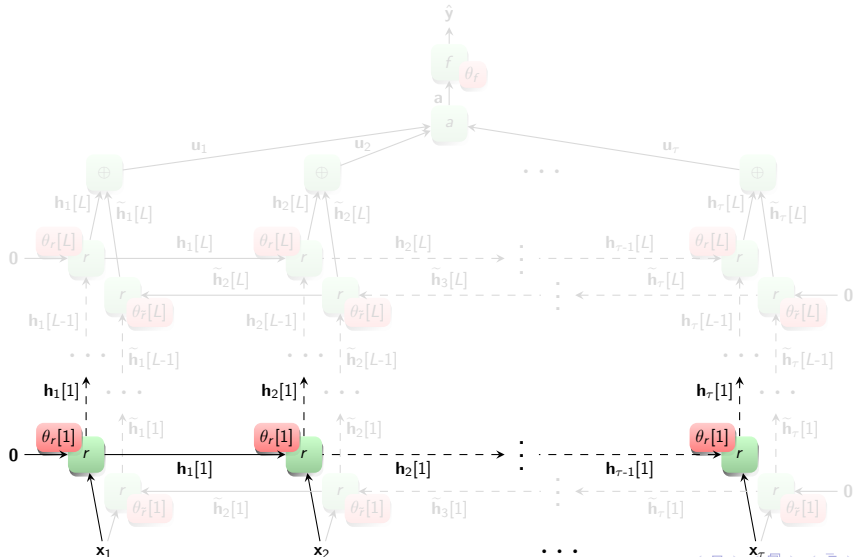
GRU



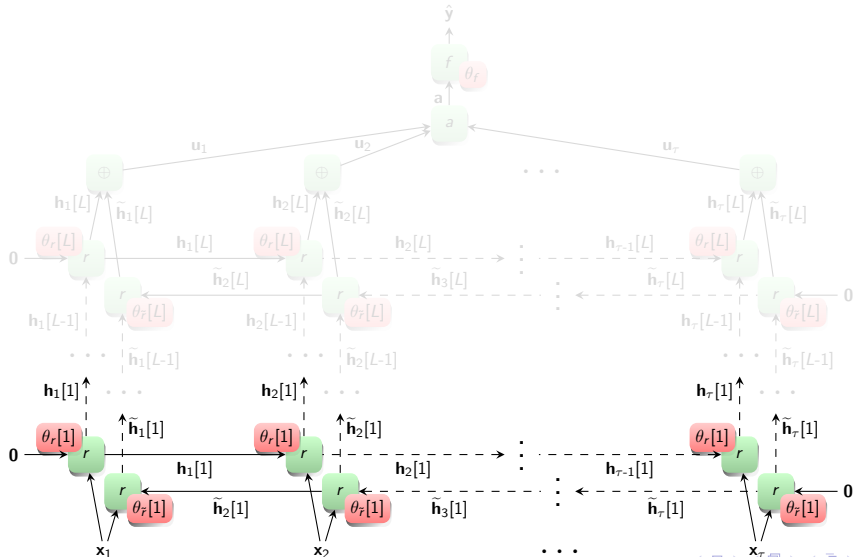
Bidirectional RNN with aggregation



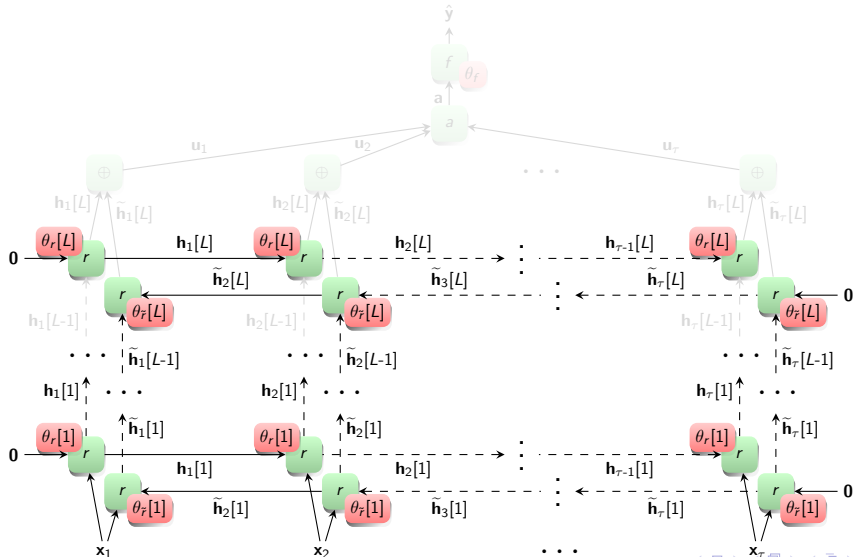
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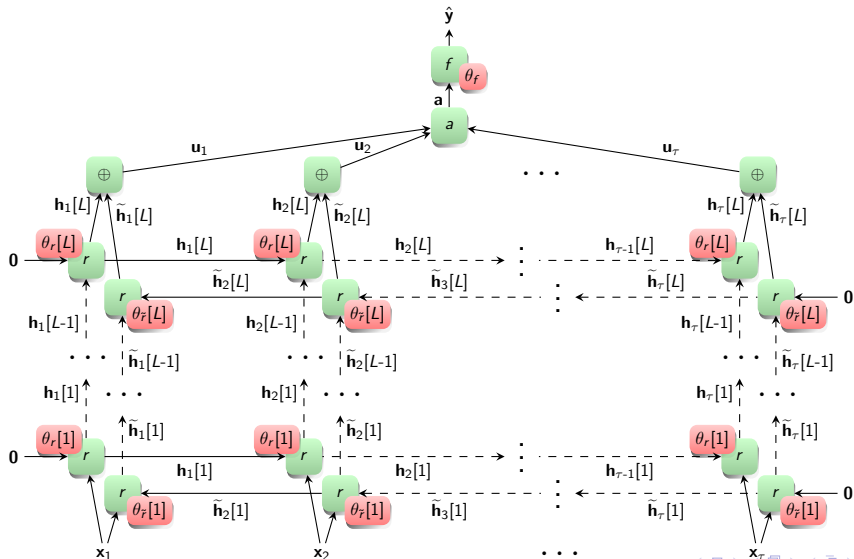
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Standard

$$\mathbf{a} = \mathbf{h}_t[L] \oplus \tilde{\mathbf{h}}_1[L]$$

Max pooling

$$\mathbf{u}_t = \mathbf{h}_t[L] \oplus \tilde{\mathbf{h}}_t[L]$$
$$\mathbf{a}^{(j)} = \max_t \mathbf{u}_t^{(j)}$$

Attention mechanism

$$\mathbf{u}_t = \mathbf{h}_t[L] \oplus \tilde{\mathbf{h}}_t[L]$$

$$\mathbf{v}_t = \tanh(\mathbf{W}^T \cdot \mathbf{u}_t + \mathbf{b})$$

$$\alpha_t \equiv \frac{e^{\langle \mathbf{v}_t, \mathbf{c} \rangle}}{\sum_{j=1}^{\tau} e^{\langle \mathbf{v}_j, \mathbf{c} \rangle}}$$

$$\mathbf{a} \equiv \sum_{t=1}^{\tau} \alpha_t \mathbf{u}_t$$

Aggregation

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Results

		$t_{15} = 0.1$			$t_{15} = 1$		
		IID	NM	VS	IID	NM	VS
$\mathcal{P}_{t_{15}}$	SVM	<u>97.0</u>	<u>82.3</u>	96.5	<u>50.3</u>	<u>51.2</u>	49.5
	MLP	96.9	80.7	<u>96.6</u>	49.5	50.7	<u>50.2</u>
$\mathcal{P}_{t_0},$ $\dots,$ $\mathcal{P}_{t_{15}}$	SVM	96.4	80.1	96.3	73.6	61.9	75.0
	GRU	96.5	91.5	<u>96.7</u>	90.5	73.3	88.2
	LSTM	96.8	90.4	96.4	88.6	70.3	86.3
	bi-GRU	96.6	92.2	96.6	91.0	74.6	<u>90.6</u>
	bi-LSTM	96.7	89.7	96.5	90.8	70.6	87.2
	bi-GRU-att	<u>97.0</u>	91.6	96.1	90.9	73.4	87.9
	bi-LSTM-att	96.9	87.9	96.3	89.0	71.6	87.4
	bi-GRU-max	96.6	<u>92.6</u>	96.6	<u>91.8</u>	<u>76.1</u>	90.4
	bi-LSTM-max	96.6	91.4	96.3	91.4	74.9	89.0

- ✓ Paper in [submission](#): Stefano Martina, Stefano Gherardini and Filippo Caruso. Machine learning approach for quantum non-Markovian noise classification

Results

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	bi-GRU	96.6	92.2	96.6	91.0	74.6	<u>90.6</u>
	bi-LSTM	96.7	89.7	96.5	90.8	70.6	87.2
	bi-GRU-att	<u>97.0</u>	91.6	96.1	90.9	73.4	87.9
	bi-LSTM-att	96.9	87.9	96.3	89.0	71.6	87.4
	bi-GRU-max	96.6	<u>92.6</u>	96.6	<u>91.8</u>	<u>76.1</u>	90.4
	bi-LSTM-max	96.6	91.4	96.3	91.4	74.9	89.0

- ✓ Paper in [submission](#): Stefano Martina, Stefano Gherardini and Filippo Caruso. Machine learning approach for quantum non-Markovian noise classification

Results

		$t_{15} = 0.1$			$t_{15} = 1$		
		IID	NM	VS	IID	NM	VS
$\mathcal{P}_{t_{15}}$	SVM	<u>97.0</u>	<u>82.3</u>	96.5	<u>50.3</u>	<u>51.2</u>	49.5
	MLP	96.9	80.7	<u>96.6</u>	49.5	50.7	<u>50.2</u>
$\mathcal{P}_{t_0},$ $\dots,$ $\mathcal{P}_{t_{15}}$	SVM	96.4	80.1	96.3	73.6	61.9	75.0
	GRU	96.5	91.5	<u>96.7</u>	90.5	73.3	88.2
	LSTM	96.8	90.4	96.4	88.6	70.3	86.3
	bi-GRU	96.6	92.2	96.6	91.0	74.6	<u>90.6</u>
	bi-LSTM	96.7	89.7	96.5	90.8	70.6	87.2
	bi-GRU-att	<u>97.0</u>	91.6	96.1	90.9	73.4	87.9
	bi-LSTM-att	96.9	87.9	96.3	89.0	71.6	87.4
	bi-GRU-max	96.6	<u>92.6</u>	96.6	<u>91.8</u>	<u>76.1</u>	90.4
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Thank you! Questions?



We have many open **postdoc** positions on Quantum Machine Learning, Quantum Sensing, and more in general Quantum Information Theory in QDAB, starting at any time! If you are interested, **contact** Prof. **Filippo Caruso**:
filippo.caruso@unifi.it — qdab.org

